

**ROCHESTER INSTITUTE OF TECHNOLOGY
MICROELECTRONIC ENGINEERING**

Piezoresistance in Silicon

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Microelectronic Engineering
Rochester Institute of Technology

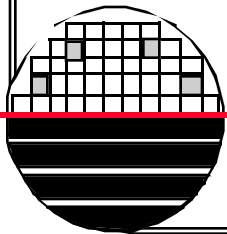
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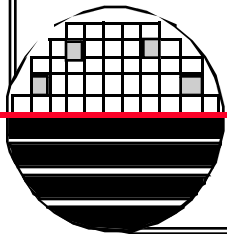
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INTRODUCTION

The piezoresistive effect was first reported in 1954 [1] and has been used in making sensors for years. The effect of strain on the mobility of electrons and holes in semiconductors is important in today's sensors and transistors.



CHARLES SMITH 1954

PHYSICAL REVIEW

VOLUME 94, NUMBER 1

APRIL 1, 1954

Piezoresistance Effect in Germanium and Silicon

CHARLES S. SMITH

Bell Telephone Laboratories, Murray Hill, New Jersey

(Received December 30, 1953)

Uniaxial tension causes a change of resistivity in silicon and germanium of both n and p types. The complete tensor piezoresistance has been determined experimentally for these materials and expressed in terms of the pressure coefficient of resistivity and two simple shear coefficients. One of the shear coefficients for each of the materials is exceptionally large and cannot be explained in terms of previously known mechanisms. A possible microscopic mechanism proposed by C. Herring which could account for one large shear constant is discussed. This so called electron transfer effect arises in the structure of the energy bands of these semiconductors, and piezoresistance may therefore give important direct experimental information about this structure.

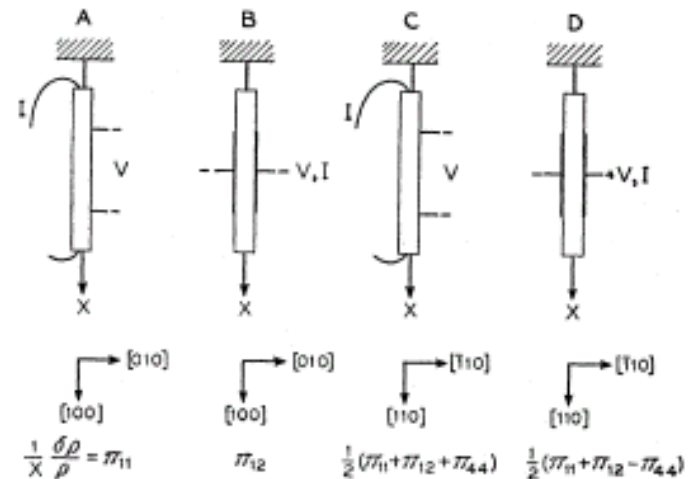
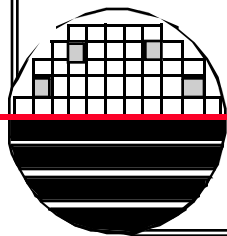


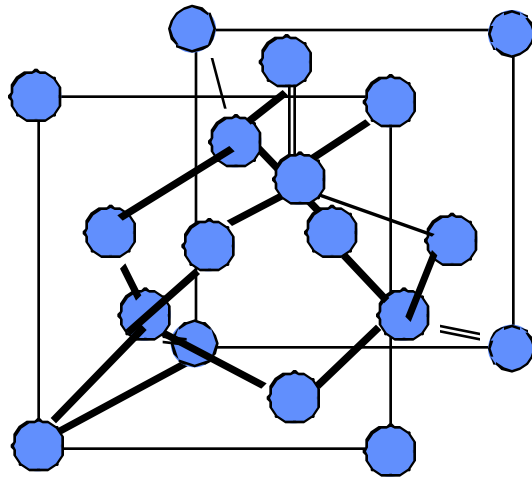
FIG. 1. Schematic diagram showing the stress system, the crystallographic orientations and the electrode structures which have been used. Arrangements A and C are designated as longitudinal in the text; B and D are called transverse.



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CRYSTAL STRUCTURE

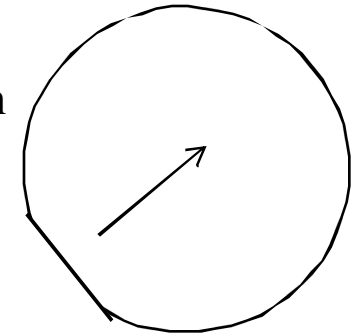
**Diamond
Lattice
(Silicon)**



● Si

**Equivalent Planes (100), (010), etc.
Directions <110>, <011>, etc.**

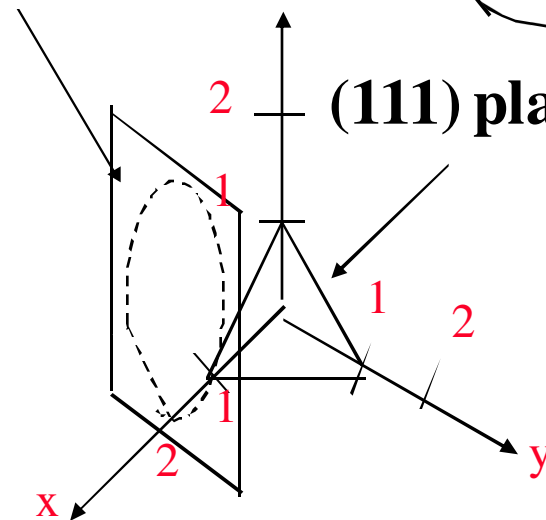
(100) wafer
<110> direction



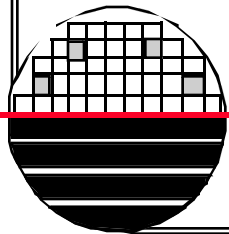
(100) plane

z

(111) plane



**Miller Indices
(1/x,1/y,1/z)
smallest integer set**



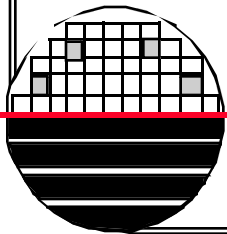
PIEZORESISTANCE

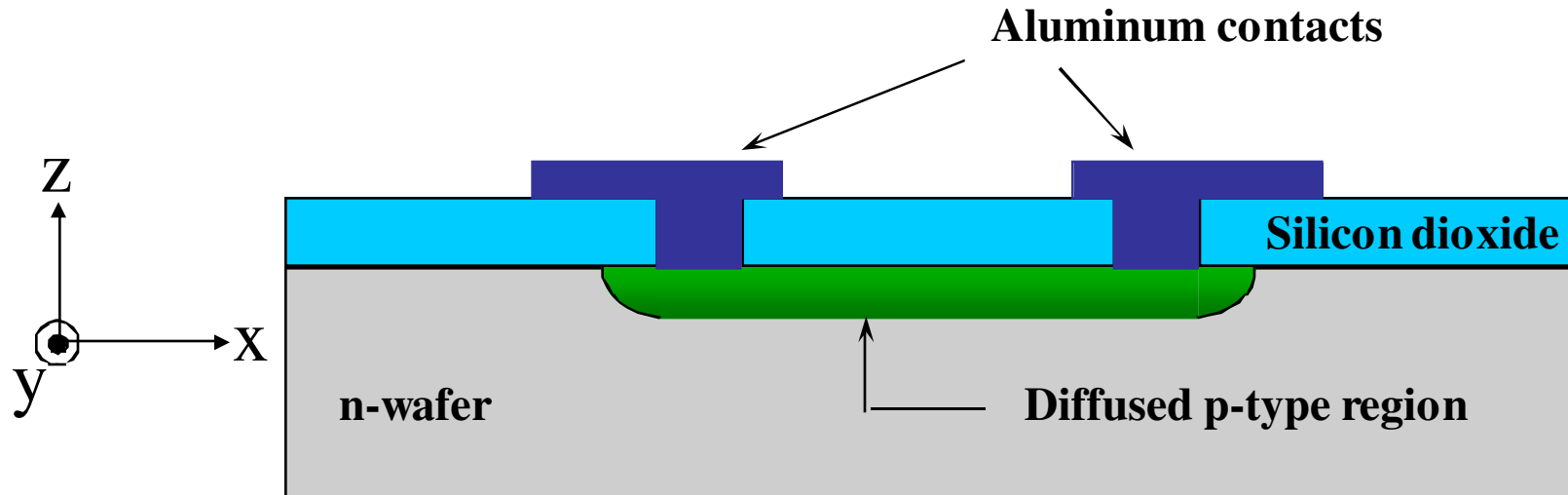
Piezoresistance is defined as the change in electrical resistance of a solid when subjected to stress. The piezoresistivity coefficient is Π and a typical value may be $1\text{E}^{-10} \text{ cm}^2/\text{dyne}$.

The fractional change in resistance $\Delta R/R$ is given by:

$$\Delta R/R = \Pi \sigma$$

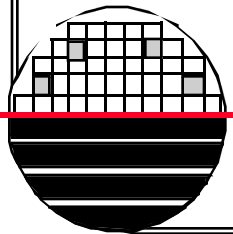
where σ is the stress in dyne/cm^2 .



SINGLE CRYSTAL DIFFUSED RESISTORS

The n-type wafer is always biased positive with respect to the p-type diffused region. This ensures that the pn junction that is formed is in reverse bias, and there is no current leaking to the substrate. Current will flow through the diffused resistor from one contact to the other. The I-V characteristic follows Ohm's Law: $I = V/R$

$$\text{Sheet Resistance} = \rho_s \sim 1/(qu \text{ Dose}) \quad \text{ohms/square}$$



EXPRESSION FOR RESISTANCE

$$R = R_0 [1 + \pi_L \sigma_{xx} + \pi_T (\sigma_{yy} + \sigma_{zz})]$$

$$R_0 = (L/W)(1/(q\mu(N,T) Dose))$$

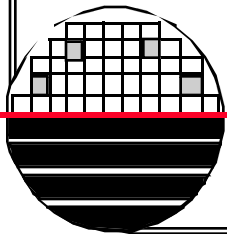
π_L is longitudinal piezoresistive coefficient

π_T is transverse piezoresistive coefficient

σ_{xx} is the x directed stress

σ_{yy} is the y directed stress

σ_{zz} is the z directed stress

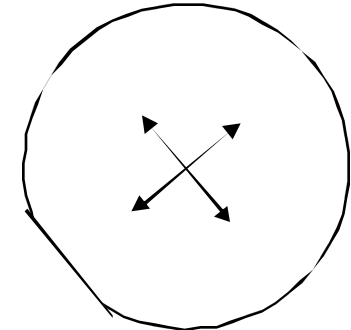


PIEZORESISTANCE COEFFICIENTS

In the $\langle 110 \rangle$ direction

	π_L (E ⁻¹¹ /Pa)	π_T (E ⁻¹¹ /Pa)
Electrons	-31.6	-17.6
holes	71.8	-66.3

(100) wafer
 $\langle 110 \rangle$ directions

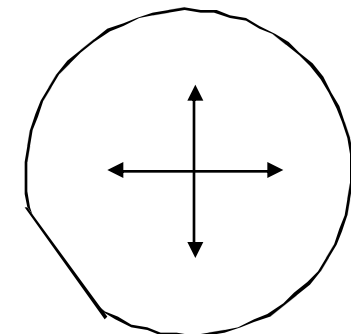


In the $\langle 100 \rangle$ direction

	π_L (E ⁻¹¹ /Pa)	π_T (E ⁻¹¹ /Pa)
Electrons	-102	53.4
holes	6.6	-1.1

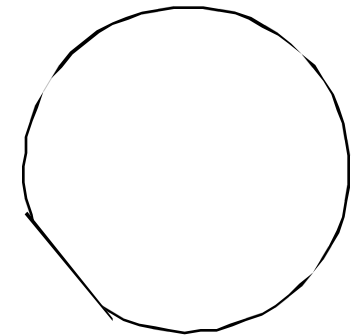
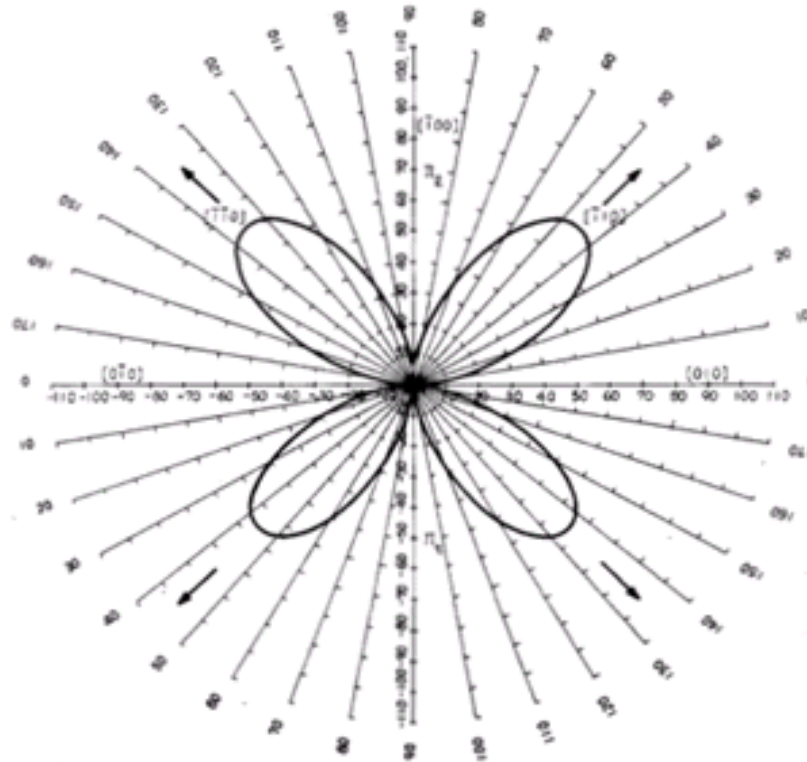
Direction of
Carrier Flow

(100) wafer
 $\langle 100 \rangle$ directions

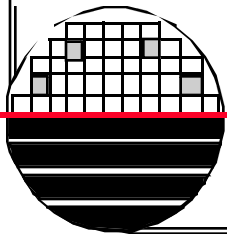


Tensile strain in (100) silicon increases mobility for electrons for flow in $\langle 110 \rangle$ direction
Compressive strain in (100) silicon increases mobility for holes for flow in $\langle 110 \rangle$ direction

PIEZORESISTANCE COEFFICIENTS VS DIRECTION



- Piezoresistance coefficients at [2] n temperature for the (001) plane of p-Si



PIEZORESISTANCE COEFFICIENTS VS DIRECTION

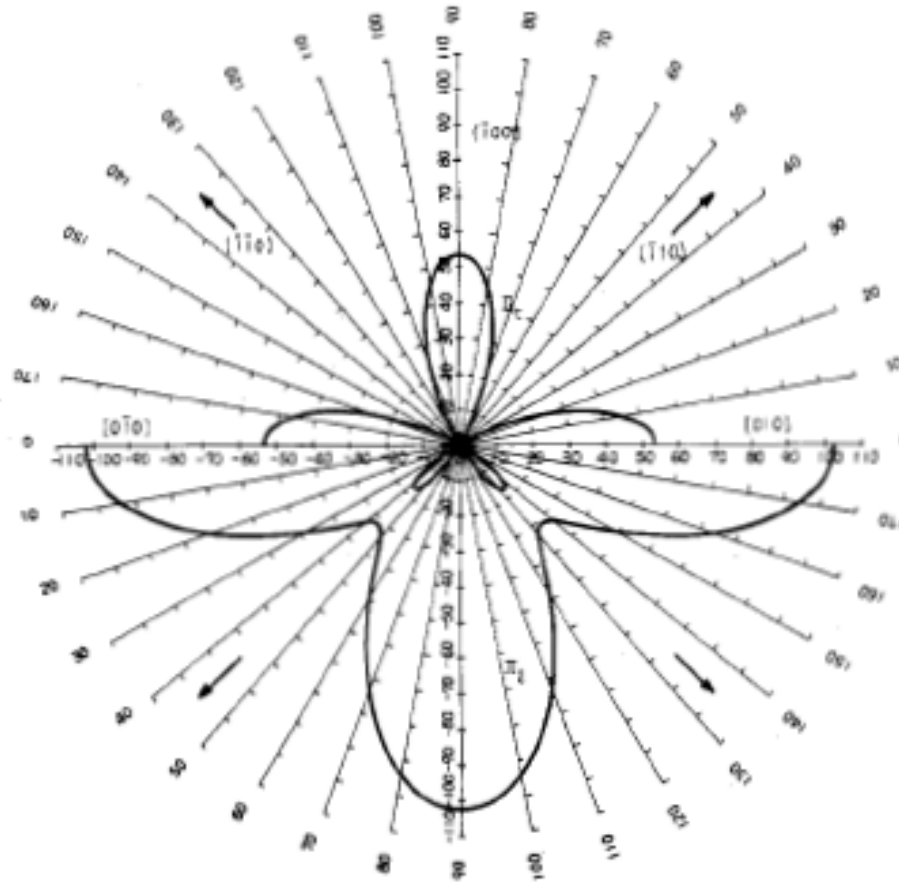
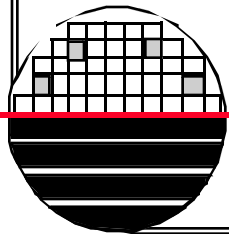


Fig. 2. Room temperature piezoresistance coefficients in the (001) plane of n-Si (10^{-12} cm²/dyne).



Roc
Mic

EXAMPLE: PIEZORESISTANCE

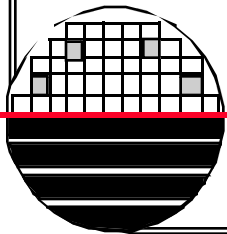
**Example: Find the maximum stress in a simple polysilicon cantilever with the following parameters.
 $Y_{\max} = 1 \mu\text{m}$, $b=4 \mu\text{m}$, $h=2\mu\text{m}$, $L=100 \mu\text{m}$**

$$\sigma_{x=0} = 5.6e7 \text{ newton/m}^2 = 5.6e8 \text{ dyne/cm}^2$$

From example in mem_mech.ppt

Continue Example: What is the change in resistance given $\Pi = 1e-10 \text{ cm}^2/\text{dyne}$

$$\begin{aligned} \Delta R/R &= \Pi \sigma = (1e-10 \text{ cm}^2/\text{dyne})(5.6e8 \text{ dyne/cm}^2) \\ &= 5.6\% \end{aligned}$$

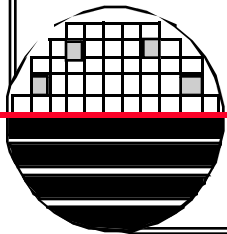


SUMMARY FOR MOBILITY / STRAIN

1. Mobility is affected by strain in semiconductors. Mobility can be increased or decreased depending on the type of strain (tensile, compressive) and the direction of strain relative to crystal orientation and current flow.

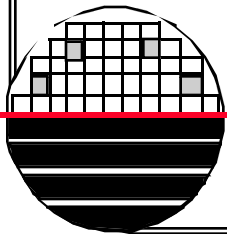
For (100) wafers and current flow in $\langle 110 \rangle$ direction:

2. Tensile strain n-type silicon enhances mobility of electrons. Tensile strain transverse to current flow enhances mobility of electrons.
3. Compressive strain in the direction of current flow in p-type silicon enhances mobility of holes. Tensile strain transverse to current flow enhances mobility of holes.



REFERENCES

1. Charles S. Smith, "Piezoresistance Effect in Germanium and Silicon," *Physical Review*, Vol 94, No.1, April 1, 1954.
2. Y. Kanda, "A graphical representation of the piezoresistance coefficients in silicon," *Electron Devices, IEEE Transactions on*, vol. 29, no. 1, pp. 64-70, 1982.
3. C. Mazure, and I. Cayrefourcq, "Status of device mobility enhancement through strained silicon engineering." pp. 1-6.
4. A. A. Barlian, W. T. Park, J. R. Mallon *et al.*, "Review: Semiconductor Piezoresistance for Microsystems," *Proceedings of the IEEE*, vol. 97, no. 3, pp. 513-552, 2009.



HOMEWORK - PIEZORESISTANCE

1. If a p-type diffused resistor on a simple cantilever experiences a tensile stress of 50 MPa what will the % change in resistance be if the resistor is oriented with its length in the same direction as the strain?
2. If a p-type diffused resistor on a simple cantilever experiences a tensile stress of 50 Mpa what will the % change in resistance be if the resistor is oriented with its width in the same direction as the strain?

